

# Ask a friend to pick a number from 1 through 1,000. After asking him ten questions that can be answered yes or no, you tell him the number. 

What kind of Questions?


## Solution:

The key to the solution is that 2 to the tenth power is $\mathbf{1 , 0 2 4}$ (that is, over 1,000). With each questions you knock out half the remaining numbers, and after ten questions only the "thought" number is left.

Say the number is 860 . The ten questions are:

1. "Is your number greater than 500?" "Yes." Add 250.
2. "Greater than 750?" "Yes." Add 125.
3. "Greater than 875 ?" "No." Subtract (not 62.5 but the nearest even number) 62 .
4. "Greater than 813 ?" "Yes." Add 31.
5. "Greater than 844 ?" "Yes."Add (not 15.5 but) 16 .
6. "Greater than 860 ?" "No." Subtract 8 .
7. "Greater than 852?" "Yes." Add 4.
8. "Greater than 856?" "Yes." Add 2.
9. "Greater than 858?" "Yes." Add 1.
10. "Greater than 859?" "Yes."

The number is 860 .
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